

Thermodynamics First Law Solved Problems

thermodynamics first law solved problems are essential for students and professionals aiming to understand the practical applications of the First Law of Thermodynamics. This fundamental principle, often referred to as the law of conservation of energy, states that energy cannot be created or destroyed in an isolated system. Instead, energy can only change forms or be transferred from one part of the system to another. Mastering solved problems related to the First Law helps in grasping complex concepts, improving problem-solving skills, and preparing for exams and real-world engineering applications. In this comprehensive article, we will explore various types of problems associated with the First Law of Thermodynamics, provide step-by-step solutions, and discuss tips to approach such problems effectively. Whether you're a beginner or looking to refine your understanding, this guide aims to serve as a valuable resource.

Understanding the First Law of Thermodynamics

Before diving into solved problems, it is crucial to understand the core concepts and equations associated with the First Law.

Basic Principles

- Energy Conservation: The total energy of an isolated system remains constant. - Forms of Energy: Includes internal energy, work done, and heat transfer. - Closed vs. Open Systems: Closed systems exchange energy but not matter; open systems exchange both.

Mathematical Expression

The First Law for a control volume or system can be written as: $\Delta U = Q - W$ Where: ΔU = Change in internal energy of the system Q = Heat added to the system W = Work done by the system For steady-flow processes, the energy balance can be expressed as: $\dot{Q} - \dot{W} = \frac{d}{dt} (U + KE + PE)$ Where KE and PE are kinetic and potential energy, respectively.

Common Types of Problems in First Law Solved Problems

Understanding the types of problems helps in developing a systematic approach. Some common problem categories include:

1. Heat transfer in closed systems
2. Work done during processes
3. Energy changes in open systems (steady-flow devices)
4. Calculations involving internal energy and enthalpy
5. Combined heat and work problems

Step-by-Step Approach to Solving First Law Problems

To solve problems efficiently, follow these steps:

1. **Identify the system:** Determine whether the problem involves a closed or open system.
2. **List knowns and unknowns:** Write down all given data and what needs to be found.
3. **Choose the appropriate energy balance equation:** Use the basic First Law expression suited to the problem.
4. **Apply relevant property data:** Use tables for internal energy, enthalpy, specific heats, etc., as needed.
5. **Perform calculations:** Solve algebraically, paying attention to units and signs.
6. **Check your results:** Verify whether the answers are physically reasonable.

Sample First Law Solved Problems with Detailed Solutions

Let's explore some typical problems to illustrate the application of the First Law.

Problem 1: Heating a Closed System

Problem Statement: A 0.5 kg aluminum block is heated in a stove from 20°C to 100°C. Assuming no heat loss, calculate the heat transferred to the aluminum. Specific heat capacity of aluminum is 900 J/kg°C. Solution: Step 1: Identify system and known data - System: Aluminum block (closed system) - Mass, $(m = 0.5\text{ kg})$ - Initial temperature, $(T_i = 20^\circ\text{C})$ - Final temperature, $(T_f = 100^\circ\text{C})$ - Specific

heat, $(c = 900 \text{ J/kg}^\circ\text{C})$ - No heat loss ($(Q_{\text{loss}} = 0)$), so heat added equals the change in internal energy. Step 2: Write the energy balance $[Q = \Delta U]$ $[\Delta U = m c (T_f - T_i)]$ Step 3: Calculate the heat transferred $[Q = 0.5 \text{ kg} \times 900 \text{ J/kg}^\circ\text{C} \times (100^\circ\text{C} - 20^\circ\text{C})]$ $[Q = 0.5 \times 900 \times 80]$ $[Q = 0.5 \times 72,000]$ $[Q = 36,000 \text{ J}]$ Answer: The heat transferred to the aluminum block is 36,000 Joules.

Problem 2: Work Done During an Isothermal Expansion

Problem Statement: An ideal gas undergoes an isothermal expansion from a volume of 2 m^3 to 5 m^3 at a temperature of 300 K . Calculate the work done by the gas. Assume the gas constant $(R = 8.314 \text{ J/mol} \cdot \text{K})$, and initial moles $(n = 1 \text{ mol})$. Solution: Step 1: Recognize the process - Isothermal process: temperature $(T = 300 \text{ K})$ - No change in internal energy for an ideal gas during isothermal process. Step 2: Write the work done formula $[W = nRT \ln \left(\frac{V_f}{V_i}\right)]$ Step 3: Substitute known values $[W = 1 \times 8.314 \times 300 \times \ln \left(\frac{5}{2}\right)]$ $[W = 8.314 \times 300 \times \ln(2.5)]$ $[W = 2494.2 \times 0.9163]$ (since $(\ln 2.5 \approx 0.9163)$) $[W \approx 2286.8 \text{ J}]$ Answer: The work done by the gas during the expansion is approximately 2287 Joules.

Advanced Problems and Applications

Beyond basic problems, real-world applications often involve complex scenarios such as: - Energy analysis of turbines, compressors, and heat exchangers - Transient processes involving temperature and pressure changes - Multistage thermodynamic cycles Solving these problems requires integrating the First Law with other principles like the Second Law, entropy considerations, and fluid mechanics.

Tips for Mastering First Law Problems

- Understand the process: Is it steady, transient, adiabatic, isothermal, etc.? Choose the right approach. - Use property tables effectively: Internal energy and enthalpy data are crucial for accurate calculations. - Maintain consistent units: Be vigilant with units to avoid errors. - Draw diagrams: Visualizing processes helps in understanding energy exchanges. - Practice diverse problems: Exposure to different scenarios enhances problem-solving skills.

Conclusion

thermodynamics first law solved problems serve as a practical bridge between theoretical concepts and real-world engineering applications. By systematically approaching each problem—identifying the system, applying the correct energy balance, and utilizing property data—you can develop a strong understanding of energy interactions in thermal systems. Regular practice with varied problems not only boosts confidence but also prepares you for advanced topics and professional challenges in thermodynamics. Remember, mastery of these problems is a stepping stone toward a comprehensive understanding of energy systems critical to engineering and science.

Thermodynamics First Law Solved Problems: An Expert Review Thermodynamics is a foundational pillar of engineering and physics, governing how energy is transferred and transformed within physical systems. Among its core principles, the First Law of Thermodynamics—also known as the Law of Energy Conservation—serves as the bedrock for analyzing energy exchanges in a variety of practical scenarios. To truly master this principle, solving diverse problems is essential, and in this article, we delve into the intricacies of first law solved problems, offering an expert perspective that combines theoretical understanding with practical application.

Understanding the First Law of Thermodynamics

Before exploring problem-solving techniques, establishing a clear understanding of the First Law is vital.

Fundamental Concept

The First Law states that energy cannot be created or destroyed; it can only be transferred or converted from one form to another. In thermodynamics, this principle is expressed mathematically as: $\Delta U = Q - W$ where: - ΔU : Change in internal energy of the system - Q : Heat added to the system - W : Work done by the system This equation encapsulates the energy balance within a system, considering heat transfer and work interactions.

Types of Processes Addressed

The Law applies to various thermodynamic processes: - Isothermal (constant temperature) - Adiabatic (no heat transfer) - Isobaric (constant pressure) - Isochoric (constant volume) - Polytropic processes Each process has specific characteristics influencing how the first law is applied.

Key Components of Solved Problems

When approaching first law problems, some common components recur: 1. Defining the System and Surroundings: Clearly identify what constitutes the system. 2. Establishing Known Data: Temperatures, pressures, volumes, heat transfer, work done. 3. Choosing Appropriate Equations: Based on the process and data. 4. Applying Conservation of Energy: Using the first law to relate variables. 5. Performing Calculations: Solving algebraically or via graphical methods. 6. Validating Results: Ensuring physical consistency and unit correctness.

Common Types of First Law Problems and How to Solve Them

Let's explore typical problem types, detailed solution approaches, and examples.

1. Closed System with Fixed Mass

Scenario: A rigid container with a fixed amount of gas undergoes heating. The problem involves calculating the change in internal energy or the work done. Solution Approach: - Identify the process: Is it heating at constant volume? Then, work $W = 0$. - Apply the First Law: $\Delta U = Q - W$ - Use standard relations: For ideal gases, $\Delta U = m c_v \Delta T$. Example: A rigid steel container contains 2 kg of air at 300 K. It is heated so that the temperature rises to 350 K. Find the increase in internal energy. Solution: - (c_v) for air ≈ 0.718 kJ/kg·K - $(\Delta T = 50, K)$ $\Delta U = m c_v \Delta T = 2, \text{kg} \times 0.718, \text{kJ/kg} \times 50, K = 71.8, \text{kJ}$ Since the container is rigid, $W = 0$, and $Q = \Delta U = 71.8$ kJ.

2. Open System with Mass Flow

Scenario: A boiler supplies steam at a certain rate, and the problem involves calculating the energy transfer rates. Solution Approach: - Apply the steady-flow energy equation: $\dot{Q} - \dot{W}_s = \dot{m} (h_{\text{out}} - h_{\text{in}} + \frac{v_{\text{out}}^2 - v_{\text{in}}^2}{2} + g(z_{\text{out}} - z_{\text{in}}))$ - Often, kinetic and potential energy changes are negligible, simplifying calculations. Example: Steam enters a turbine at 3 MPa, 500°C with a mass flow rate of 2 kg/s. The exhaust pressure is 10 kPa. Assuming negligible kinetic and potential energy changes, find the rate of heat transfer if the specific enthalpy at inlet and outlet are 3300 kJ/kg and 2200 kJ/kg, respectively. Solution: $\dot{Q} = \dot{m} (h_{\text{out}} - h_{\text{in}}) = 2, \text{kg/s} \times (2200 - 3300), \text{kJ/kg} = -2200, \text{kW}$ Negative sign indicates heat is lost (removed) from the system.

3. Polytropic Process in a P-V Diagram

Scenario: A gas undergoes a polytropic process, and the problem involves calculating work done or heat transfer. Solution Approach: - Use the relation: $PV^n = \text{constant}$ - The work done: $W = \frac{P_2 V_2 - P_1 V_1}{1 - n}$ - The heat transfer: $Q = \Delta U + W$ - For an ideal gas: $\Delta U = m c_v (T_2 - T_1)$ Example: Air expands from 1 MPa and 0.1 m³ to 0.2 m³, with a polytropic index $n=1.3$. Find the work done and heat transfer. Solution: - Find initial temperature (T_1): $PV = mRT \rightarrow T_1 = \frac{PV}{mR}$ - Assuming 1 mol of air for simplicity: $R = 8.314 \text{ J/mol}\cdot\text{K}$ $T_1 = \frac{1 \times 10^6 \text{ Pa} \times 0.1 \text{ m}^3}{1 \times 8.314 \text{ J/mol}\cdot\text{K}} \approx 12030 \text{ K}$ - Find (P_2, V_2): $V_2 = 0.2 \text{ m}^3$ - Using the polytropic relation: $P_2 = P_1 \left(\frac{V_1}{V_2}\right)^n = 1 \text{ MPa} \times \left(\frac{0.1}{0.2}\right)^{1.3} \approx 1 \text{ MPa} \times (0.5)^{1.3} \approx 1 \text{ MPa} \times 0.406 \approx 0.406 \text{ MPa}$ - Find (T_2): $T_2 = \frac{P_2 V_2}{mR} \approx \frac{0.406 \times 10^6 \text{ Pa} \times 0.2 \text{ m}^3}{1 \times 8.314 \text{ J/mol}\cdot\text{K}} \approx 9770 \text{ K}$ - Calculate work: $W = \frac{P_2 V_2 - P_1 V_1}{1 - n} = \frac{(0.406 \times 10^6 \times 0.2) - (1 \times 10^6 \times 0.1)}{1 - 1.3} = \frac{81,200 - 100,000}{-0.3} \approx \frac{-18,800}{-0.3} \approx 62,667 \text{ J}$ - Change in internal energy: $\Delta U = m c_v (T_2 - T_1)$ Assuming ($c_v \approx 0.718 \text{ kJ/kg}\cdot\text{K}$): $\Delta U = 1 \text{ kg} \times 0.718 \text{ kJ/kg}\cdot\text{K} \times (9770 - 12030) \text{ K} \approx 0.718 \times (-2260) \approx -1622 \text{ kJ}$ - Heat transfer: $Q = \Delta U + W \approx -1622 \text{ kJ} + 62.7 \text{ kJ} \approx -1559 \text{ kJ}$ Indicating heat is removed from the system.

Best Practices for Solving First Law Problems

To achieve accuracy and efficiency, consider these expert tips: - Clearly define the system: Is it open or closed? What are the boundary conditions? - Identify the process type: Is it isothermal, adiabatic, etc.? This simplifies equations. - Use appropriate property data: Consult steam tables, property charts, or ideal gas relations. - Maintain consistent units: SI units are standard; convert all data accordingly. - Check assumptions: Are kinetic and potential energy changes negligible? Clarify before applying formulas. - Diagram your process: P-V, T-S, or T-V diagrams help visualize energy exchanges. - Validate results: Confirm physical plausibility—e.g., energy increases in heating.

Advanced Problem-Solving Strategies

Questions & Answers About thermodynamics first law solved problems

No	Question	Answer
1	What is the first law of thermodynamics and how is it applied in solving problems?	The first law of thermodynamics states that energy cannot be created or destroyed, only transferred or converted. In solving problems, it is applied by accounting for the heat added to or removed from a system and the work done by or on the system to determine changes in internal energy.
2	How do you solve a problem involving a gas undergoing an isothermal process using the first law?	In an isothermal process, the temperature remains constant, so the change in internal energy is zero. The first law simplifies to $Q = W$, meaning the heat added to the system equals the work done by the system. You can then calculate either heat or work using the appropriate formulas for the process.
3	What is a common approach to solving first law problems involving a cyclic process?	For cyclic processes, the net change in internal energy over one complete cycle is zero. Therefore, the net heat transfer equals the net work done over the cycle ($Q_{\text{net}} = W_{\text{net}}$). This simplifies the analysis by focusing on the total heat and work over the cycle.
4	How do you handle first law problems involving multiple steps, such as heating followed by expansion?	Break down the process into individual steps, apply the first law to each step separately, and then sum the results. Track heat transfer and work for each step, ensuring energy conservation across the entire process to find the overall change in internal energy or other desired variables.
5	When solving a problem involving an ideal gas, what specific considerations are important in applying the first law?	For ideal gases, internal energy depends only on temperature. When applying the first law, use the relation $\Delta U = nC_v\Delta T$ for changes in internal energy, and relate heat and work to pressure, volume, and temperature changes using ideal gas law equations to simplify calculations.
6	What are some common mistakes to avoid when solving first law thermodynamics problems?	Common mistakes include neglecting units, mixing up heat and work terms, assuming incorrect process types, ignoring state variables, or not accounting for the direction of heat flow and work. Carefully defining system boundaries and clearly identifying each energy transfer helps avoid errors.

thermodynamics, first law, energy conservation, heat transfer, work done, internal energy, solved problems, heat engines, energy analysis, thermodynamic processes